

**University of Bahrain**  
**College of Information technology**  
**Department of Computer Engineering**

**Test (1)**

Student Name	
I.D. No.	<i>Solution</i>
Section	

**Course Title:** Digital Logic  
**Course number:** ITCE 202/250  
**Semester:** 1  
**Academic Year:** 2013/2014  
**Duration :** 1hour  
**Date:** 29/10/2013

**Read the following before you start:**

1. Write your name, ID and section number
2. Answer all questions.
3. Write your answers on the attached sheets only.

Question	Mark	Mark attained
1	22	
2	16	
3	15	
4	22	
5	25	
Total	100	

**Question [1]: [22 mark]**

(a) Convert the following numbers showing all steps.

3  $(1111)_2 = ( )_{BCD} \quad 15_{10} = 0001 \ 0101_{BCD}$

3  $(A29)_{16} = ( )_4$

1	0	1	0	0	0	1	0	1	0	0	1
2	2	0	2	2	2	1	4				

3  $(15)_{10} = ( )_{\text{excess}_3}$

$0001 \ 0101_{BCD} \xrightarrow{+3} 0100 \ 1000_{\text{excess}_3}$

3  $(-35)_{10} = ( )_{1's \text{ complement}}$

	64	32	16	8	4	2	1
Binary +35	0	1	0	0	0	1	1
1's Comp -35	1	0	1	1	1	0	0

(b) Add the following numbers in BCD

5  $(97)_{10} + (25)_{10} =$

1	0	0	1	0	1	1	1	97
0	0	1	0	0	1	0	1	25
<hr/>								
1	0	1	1	1	0	0	0	122
0	1	1	0	0	1	1	0	
<hr/>								
0	0	0	1	0	0	1	0	

5 b) Perform the following operation using 6-bit 2's complement numbers and indicate the case of an overflow.

$(-20)_{10} + (-15)_{10} =$

	32	16	8	4	2	1
+20	0	1	0	1	0	0
+15	0	0	1	1	1	1

-20	1	0	1	1	0	0
-15	1	1	0	0	0	1
	<hr/>					
-35	1	0	1	1	0	1
	<hr/>					
	C=1					
	V=1					

## Question [2]: [16 mark]

1. Simplify the following expression using the Boolean algebra to a minimum number of literals:

$$\overline{A + B} + ABC + A\overline{B}$$

$$\overline{A}\overline{B} + ABC + A\overline{B}$$

$$\overline{B}(\overline{A} + A) + ABC$$

$$\overline{B} + ABC$$

$$\overline{B} + AC$$

- 2- Find the minimum Product of Sum for the following function, use Boolean Algebra.

$$(a+b)(a+b+d)(a+c)$$

$$\overline{F} = \overline{a}\overline{b} + \overline{a}\overline{b}\overline{d} + \overline{a}\overline{c}$$

$$= \overline{a}\overline{b}(1 + \overline{d}) + \overline{a}\overline{c}$$

$$= \overline{a}\overline{b} + \overline{a}\overline{c}$$

$$F = (a+b)(a+c)$$

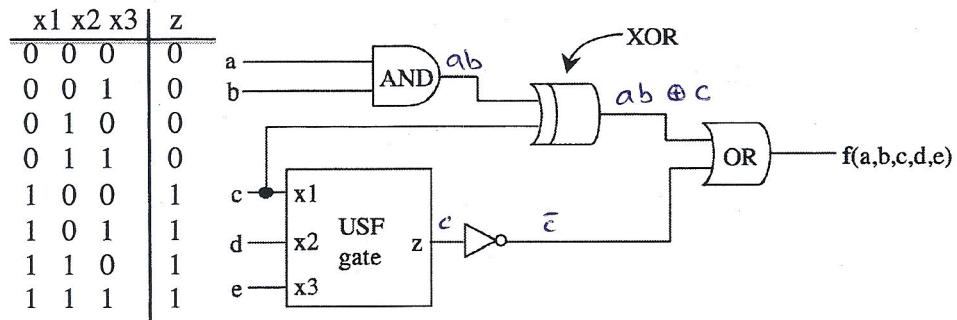
cd \ ab	00	01	11	10
00	0	0		
01	0	0		
11	0			
10	0			

$$\overline{F} = \overline{a}\overline{b} + \overline{a}\overline{c}$$

OR use  $X \cdot (X + Y) = X$  ← Theorem 10D on Page 52  
 to get  $(a+b)(a+b+d)(a+c)$   
 $= (a+b)(a+c)$

**Question [3]: [15 mark]**

In the given circuit below, the gate labeled “USF gate” has the truth table shown below.



Write  $f(a,b,c,d,e)$  as a minimum sum of product.

③  $z = c$

⑤  $f = (ab \oplus c) + \bar{z}$

$= ab\bar{z} + \bar{a}\bar{b}\bar{z} + \bar{z}$

$= ab\bar{z} + c(\bar{a} + \bar{b}) + \bar{z}$

$= ab\bar{z} + \bar{a}c + \bar{b}c + \bar{z}$

$= \bar{z}(ab + 1) + \bar{a}c + \bar{b}c$

$= \bar{z} + \bar{a}c + \bar{b}c$

$= \bar{z} + \bar{a} + \bar{b}c$

$= \bar{a} + \bar{b} + \bar{z}$

ab \ c	0	1
00	1	1
01	1	1
11	1	0
10	1	1

$\bar{a} + \bar{b} + \bar{z}$

**Question [4]: [22 mark]**

a-- Find the maxterm expansion in algebraical expansion (in complete form) of the following expression:

$$F(X, Y, Z) = XY + \bar{X}Z + X\bar{Y}\bar{Z}$$

$$F = \sum m(1, 3, 4, 6, 7)$$

$$= \prod M(0, 2, 5)$$

$$\bar{F} = \bar{X}\bar{Y}\bar{Z} + \bar{X}Y\bar{Z} + X\bar{Y}Z$$

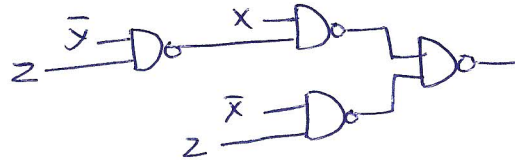
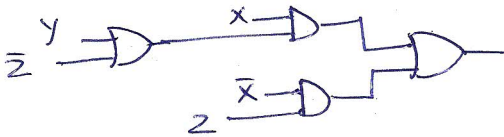
$$F = (X + Y + Z)(X + \bar{Y} + Z)(\bar{X} + Y + \bar{Z})$$

$Y \backslash X$	0	1		
0	0	1		
1	1	0		
1	1	1		
0	0	1		

b-- Implement F using minimum 2-inputs NAND gates.

$$F = XY + \bar{X}Z + X\bar{Z}$$

$$= X(Y + \bar{Z}) + \bar{X}Z$$



C -- Write  $F(a, b, c, d) = \sum m(5, 6, 7, 8, 9, 10, 11, 12, 13, 15) + \sum d(0, 3, 14)$  as minimum sum of product.

$$F = a + bd + bc$$

$cd \backslash ab$	00	01	11	10
00	X		1	1
01		1	1	1
11	X	1	1	1
10		1	X	1

**Question [5]: [25 mark]**

A combinational logic circuit receives BCD numbers as input. The output (W, X, Y, Z) represents the excess-3 code of the inputs. Consider the invalid inputs as don't care cases.

- (a) Construct the truth table.  
 (b) Find the minterm expansion of W in decimal notation.  
 (c) Find the maxterm expansion of X in decimal notation.  
 (d) Find the minimum SOP expression of Z.  
 (e) Implement Y using minimum number of NOR gates only.

b)  $W = \sum m(5, 6, 7, 8, 9) + \sum d(10, 11, 12, 13, 14, 15)$

c)  $X = \prod M(0, 5, 6, 7, 8) \cdot \prod D(10, 11, 12, 13, 14, 15)$

d)

AB \ CD	00	01	11	10
00	1	1	X	1
01	0	0	X	0
11	0	0	X	X
10	1	1	X	X

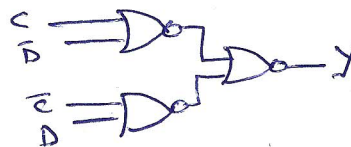
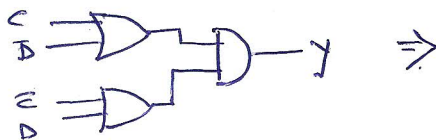
$Z = \bar{D}$

e)

AB \ CD	00	01	11	10
00	1	1	X	1
01	0	0	X	0
11	1	1	X	X
10	0	0	X	X

$\bar{Y} = \bar{C}D + C\bar{D}$

$Y = (C + \bar{D})(\bar{C} + D)$



a)

	A	B	C	D	W	X	Y	Z
0	0	0	0	0	0	0	1	1
1	0	0	0	1	0	1	0	0
2	0	0	1	0	0	1	0	1
3	0	0	1	1	0	1	1	0
4	0	1	0	0	0	1	1	1
5	0	1	0	1	1	0	0	0
6	0	1	1	0	1	0	0	1
7	0	1	1	1	1	0	1	0
8	1	0	0	0	1	0	1	1
9	1	0	0	1	1	1	0	0
	1	0	1	0	X	X	X	X
	1	0	1	1	X	X	X	X
	1	1	0	0	X	X	X	X
	1	1	0	1	X	X	X	X
	1	1	1	0	X	X	X	X
	1	1	1	1	X	X	X	X